

# Circular Motion

circular motion; *a.k.a.* “curvi-linear motion” ---> where direction changes continuously

uniform circular motion ----> when an object moves in a circular path with constant speed. [ex.'s: blades of a fan, hands of a clock]

## *Is the velocity of moving object constant? Is it accelerating?*

Remember! speed  $\neq$  velocity ----> vector (magnitude & direction)

\*Changing either changes velocity, and object is thus accelerating!

\*Because the direction is changing, it must be acted on by an unbalanced force ( $F_c$ ), and therefore will accelerate according to Newton's laws of motion.

*Which direction is the object accelerating?* The direction of acceleration is in the direction of ( $F_c$ ).

While ( $v$ ) is tangential to circular path, ( $a$ ) is toward the center --- “centripetal acceleration” ( $a_c$ ).

$$a_c = v_r^2 / r$$

ex; A race car travels 45 m/s around a circular track whose radius is 350 meters. What is the car's ( $a_c$ )?

sol;  $a_c = v_r^2 / r = 5.8 \text{ m/s}^2$

ex; The moon travels at 1,022 m/s around the earth with radius of 382,176,000 m. What is the moon's ( $a_c$ )?

sol;  $a_c = v_r^2 / r = 0.0027 \text{ m/s}^2$  (This value multiplied by 3,600 is equal to  $9.8 \text{ m/s}^2$ .)

## *How can we determine centripetal forces?*

Use Newton's 2<sup>nd</sup> law:  $F_c = ma_c = mv_r^2 / r$

ex; A 5 kg object moves with a tangential velocity of 20 m/s around the center of a circle whose radius is 25 m.

a) What is ( $a_c$ )? sol;  $a_c = v_r^2 / r = 16 \text{ m/s}^2$

b) What is the centripetal force ( $F_c$ ) required to keep this object in a circular motion?

sol;  $F_c = ma_c = 80 \text{ N}$

ex; What is the  $F_c$  which holds the moon in orbit? Mass of moon ( $m_m$ ) =  $7.35 \times 10^{22} \text{ kg}$

sol;  $F_c = (m_m)a_c \text{ ----> } (7.35 \times 10^{22} \text{ kg})(0.0027 \text{ m/s}^2) = 1.98 \times 10^{20} \text{ N}$

**centrifugal effect** (“force”) ---> The *apparent* force directed radially outward from the center (“center-fleeing”).

-This *apparent* force is equal and opposite to the inward ( $F_c$ ).

-It is a pseudo-force because it is not caused by any force, but rather by the objects' inertial straight-line motion.